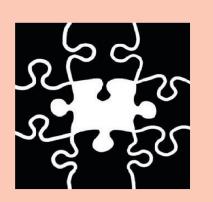
-two minus -four) minus one) plus seven) plus -one) (nine plus -six) ((eight minus (six minus zero)) minus -nine) plus zero) one (-six minus

# Diagnostic Classifiers:

# Revealing how Neural Networks process Hierarchical Structure



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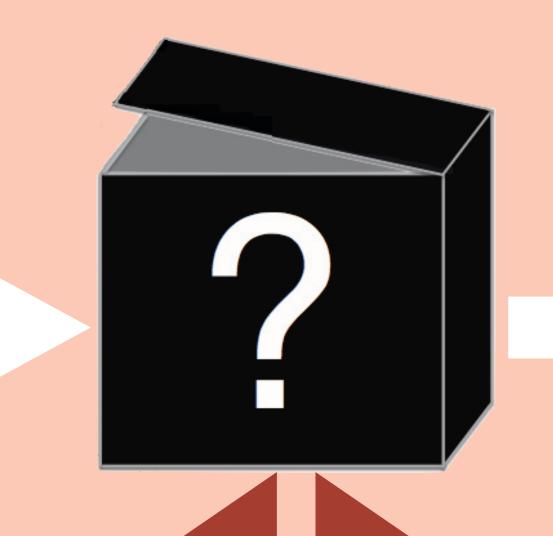
four minus -five ) minus (zero minus -three ) ) ( (-nine minus -one ) minus (seven plus one ) ) -five -eight ( (five plus three ) plus

We analyse how recursive and recurrent neural networks perform a task that involves hierarchical compositional semantics. The solution of the recursive network can be understood through visual inspection. The solution of the recurrent network by training diagnostic classifiers: models that predict features from the hidden representations.

### Arithmetic Language

Sentences consist of digits and operators. Brackets indicate compositional structure.

> ((-two minus (two plus three)) minus (six plus one))



## Training signal

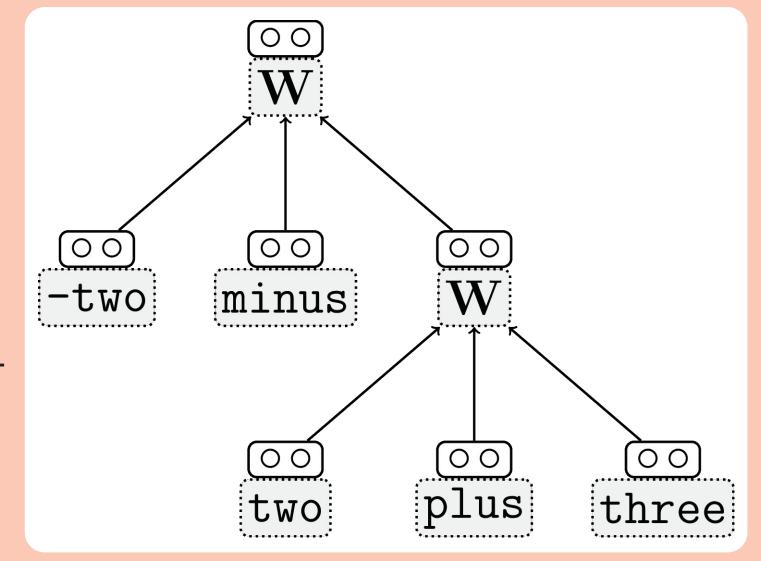
three plus zero ) minus ( three plus -four ) ) ) plus ( -three minus ( three p

The solution to the arithmetic expression defines its semantics

o minus -six ) plus two ) ) plus ( -seven plus ( eight minus four ) ) ) plus -twa

# Recursive Neural Network (TreeRNN)

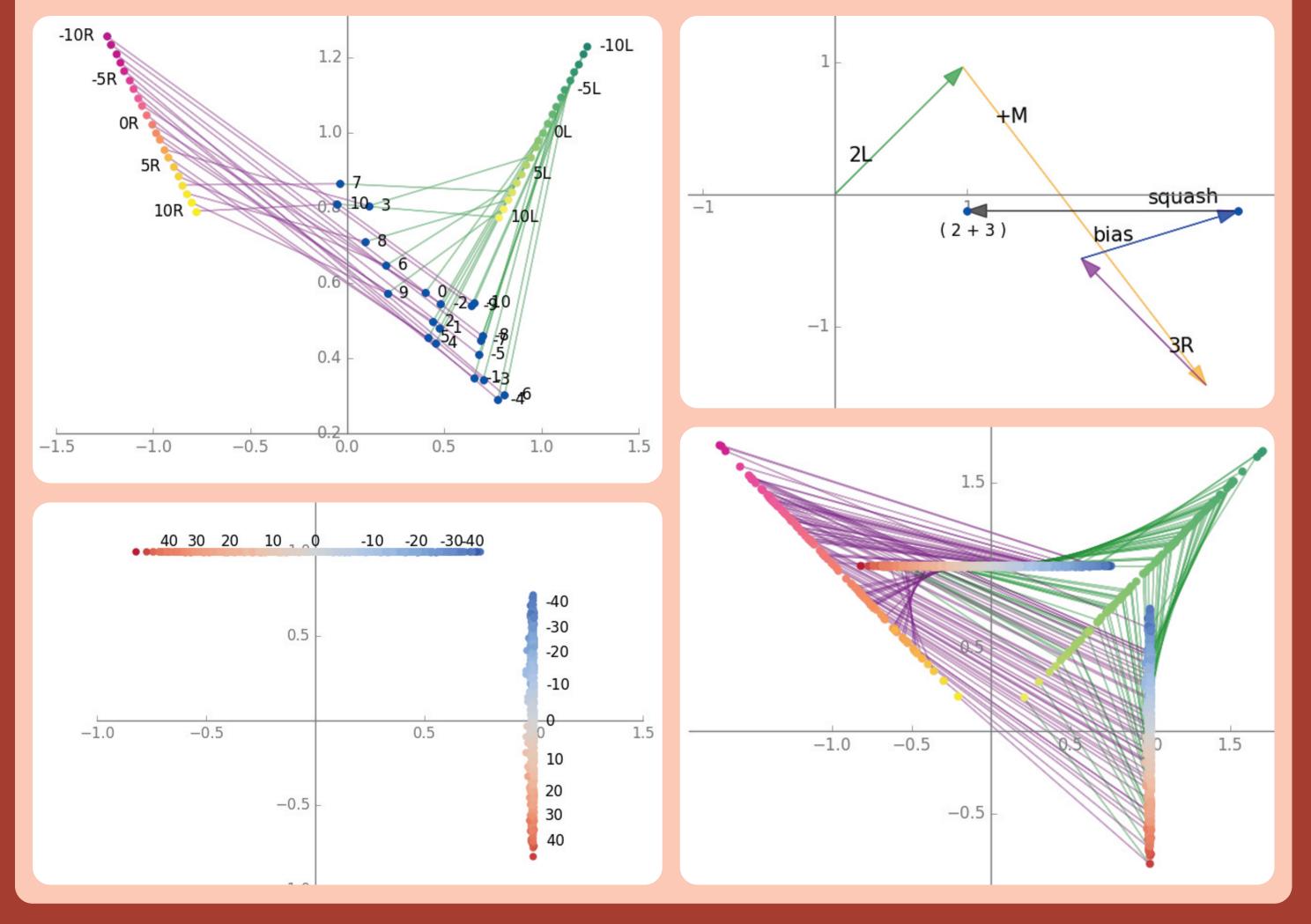
The architecture of the TreeRNN [1] mirrors the syntactic structure of the sentence. A single composition function is applied recursively to compute a vectorial parent representation from concatenated children representations:



$$\mathbf{p} = \tanh(\mathbf{W}_L \cdot \mathbf{x}_1 + \mathbf{W}_M \cdot \mathbf{x}_2 + \mathbf{W}_R \cdot \mathbf{x}_3 + \mathbf{b})$$

### Project - Sum - Squash

By plotting the 2D representations we get full understanding of the learned solution. Each child representation is projected by either W<sub>I</sub>, W<sub>M</sub> or W<sub>R</sub>. The projections are summed together with the bias. The result is squashed through tanh.



#### References

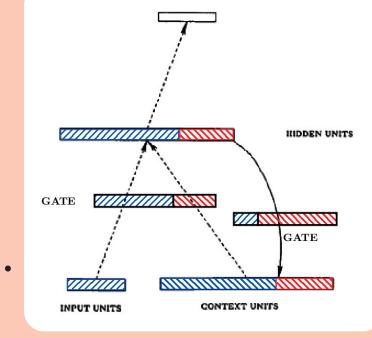
[1] Socher et al. Learning continuous phrase representations and syntactic parsing with recursive neural networks. NIPS-2010. DL and Unsup Feat. Learning Workshop, pages 1-9, 2010.

[2] Cho et al. On the properties of neural machine translation: encoderdecoder approaches. SSST-8. 2014.

[3] Elman. Finding structure in time. Cognitive Science. 1990. 14, 2.

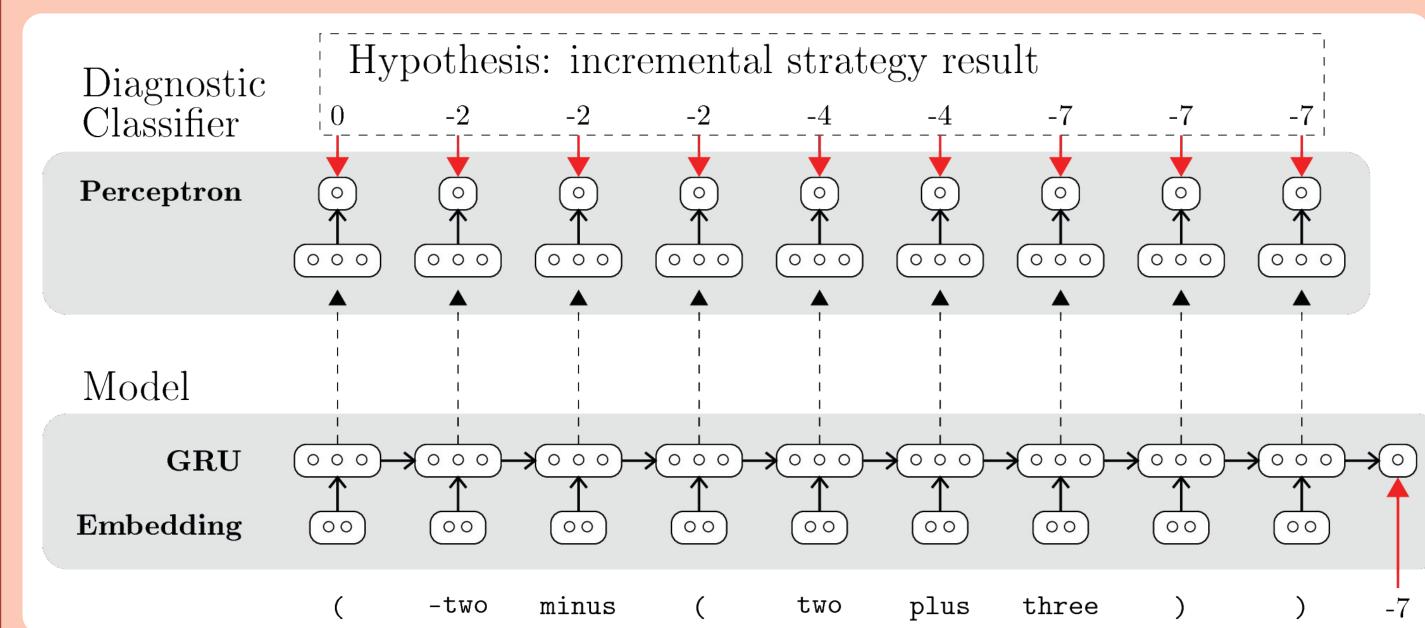
Gated Recurrent Neural Network (GRU)

The GRU [2] processes input sequences incrementally, employing gates to moderate the information flow. Brackets are inputted as words indicating the compositional structure of input sequences.



## Diagnostic Classifiers

We train additional neural networks to predict hypothesised features from the hidden representations.



#### Trajectories

If blus -ten | | -six blus six | minus | six blus -seven | blus -eight | minus | seven blus | -six minus -six | minus -six | blus | two minus | -two min

We train diagnostic classifiers to predict the intermediate resuls of two different symbolic strategies. We find that the network does not compute the outcome of the expression in a linearised recursive fashion, but integrates the digits incrementally without employing a 'result-stack' of numeric values.

