## On neural networks and compositionality

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## Neural networks and Compositionality

- Why do I care about neural networks?
- Why do I care about compositionality?



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# Neural networks and Compositionality

- Why do I care about neural networks?
- Why do I care about compositionality?
- What do these two things have to do with each other?

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 "Modern approaches [...] do not explicitly formulate and execute compositional paths" (Johnson et al., 2017) Testing compositionality

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- "Modern approaches [...] do not explicitly formulate and execute compositional paths" (Johnson et al., 2017)
- "Neural network models lack the ability to extract systematic rules" (Lake and Baroni, 2018)

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- "Modern approaches [...] do not explicitly formulate and execute compositional paths" (Johnson et al., 2017)
- "Neural network models lack the ability to extract systematic rules" (Lake and Baroni, 2018)
- "They do not learn in a compositional way" (Liška et al., 2018)

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- "Modern approaches [...] do not explicitly formulate and execute compositional paths" (Johnson et al., 2017)
- "Neural network models lack the ability to extract systematic rules" (Lake and Baroni, 2018)
- "They do not learn in a compositional way" (Liška et al., 2018)
- "[...] neural networks are essentially very large correlation engines that hone in on any statisctical, potentially spurious pattern" (Hudson and Manning, 2018)

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- "Modern approaches [...] do not explicitly formulate and execute compositional paths" (Johnson et al., 2017)
- "Neural network models lack the ability to extract systematic rules" (Lake and Baroni, 2018)
- "They do not learn in a compositional way" (Liška et al., 2018)
- "[...] neural networks are essentially very large correlation engines that hone in on any statisctical, potentially spurious pattern" (Hudson and Manning, 2018)
- Neural networks are data-hungry because they don't develop re-usable representations (almost everyone)

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## The rest of the team



Mathijs Mul





# Verna Dankers

Elia Bruni

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## The principle of compositionality

The meaning of a complex expression is determined by the meanings of its constituents and by its structure Szabó (2000) Testing compositionality

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## The principle of compositionality

The meaning of a complex expression is determined by the meanings of its constituents and by its structure Szabó (2000)

The meaning of a whole is a function of the meanings of the parts and of the way they are syntactically combined. Partee (1995) Testing compositionality

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What does it mean that neural networks are not compositional?

- They find different parts than we expect
- They find different rules than we expect
- They find other aspects of the data more salient
- They cannot represent hierarchy



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What does it mean that neural networks are not compositional?

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- They find different parts than we expect
- They find different rules than we expect
- They find other aspects of the data more salient

- They favour modelling exceptions over learning rules
- They are not getting the right signal from the data
- The 'test' data is distributionally too different from the training data

Our approach: "dissect" compositionality:

Does a model find the right parts and rules?



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## Our approach: "dissect" compositionality:

- Does a model find the right parts and rules?
- Does a model use the parts and rules it finds systematically



## Our approach: "dissect" compositionality:

- Does a model find the right parts and rules?
- Does a model use the parts and rules it finds systematically
- Does a model use the parts and rules it finds productively



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### Our approach: "dissect" compositionality:

- Does a model find the right parts and rules?
- Does a model use the parts and rules it finds systematically
- Does a model use the parts and rules it finds productively
- Does a model compute *locally consistent* representations?



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### Our approach: "dissect" compositionality:

- Does a model find the right parts and rules?
- Does a model use the parts and rules it finds systematically
- Does a model use the parts and rules it finds productively
- Does a model compute *locally consistent* representations?
- Does a model allow substitution of synonyms?

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### Our approach: "dissect" compositionality:

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- Does a model prefer rules or exceptions?

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reverse A B C



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reverse A B C  $\Rightarrow$  C B A



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 $\begin{array}{ccc} \mbox{reverse A B C} & \Rightarrow & \mbox{C B A} \\ \mbox{copy D E} \end{array}$ 

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 $\begin{array}{cccc} \mbox{reverse A B C} & \Rightarrow & \mbox{C B A} \\ \mbox{copy D E} & \Rightarrow & \mbox{D E} \end{array}$ 

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Data PCFG SET

> Unary functions: reverse, swap, copy, ... Binary functions: prepend, append, remove\_first, ... Characters: A, B, C, ...

 $\begin{array}{cccc} \mbox{reverse A B C} & \Rightarrow & \mbox{C B A} \\ \mbox{copy D E} & \Rightarrow & \mbox{D E} \\ \mbox{append C B A , D E} \end{array}$ 

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Data PCFG SET

> Unary functions: reverse, swap, copy, ... Binary functions: prepend, append, remove\_first, ... Characters: A, B, C, ...

reverse A B C	$\Rightarrow$	СВА	
сору D Е	$\Rightarrow$	DE	
append C B A , D E	$\Rightarrow$	CBADE	2



Data PCFG SET

> Unary functions: reverse, swap, copy, ... Binary functions: prepend, append, remove\_first, ... Characters: A, B, C, ...

reverse A B C $\Rightarrow$ C B Acopy D E $\Rightarrow$ D Eappend C B A , D E $\Rightarrow$ C B A D E

append reverse A B C , copy D E  $\Rightarrow$  C B A D E

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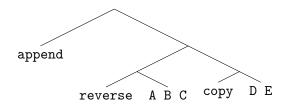
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append reverse A B C , copy D E  $\ \Rightarrow$  C B A D E



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# PCFG SET

#### Data Naturalisation

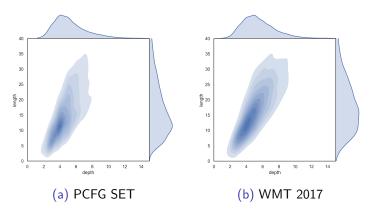


Figure: Distribution of sentence depth and length in the PCFG SET and WMT2017 data.

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## Models

# 1. LSTMS2S Recurrent encoder-decoder model with attention

- 2. **ConvS2S** Convolutional encoder and decoder with multistep attention
- 3. Transformer Fully attention based model

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## Results

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Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	$0.769\pm0.006$	$0.841 \pm 0.014$	$0.925\pm0.007$

## Systematicity

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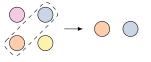
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Can models systematically recombine unseen pairs of functions?

## Results Systematicity

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Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	$0.769\pm0.006$	$0.841\pm0.014$	$0.925\pm0.007$
Systematicity*	$0.512\pm0.026$	$0.552\pm0.007$	$0.699\pm0.009$

Productivity

Can models productively combine functions to generate longer sequences?

- Newly formed sequences (generalisation)
- Combinations of known sequences (concatenation)

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## Results Productivity

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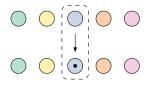
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Experiment	LSTMS2S	ConvS2S	Transformer
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Systematicity*	$0.512\pm0.026$	$0.552\pm0.007$	$0.699 \pm 0.009$
Productivity, generalisation* concatenation <sup>†</sup>	$\begin{array}{c} 0.293 \pm 0.010 \\ 0.196 \pm 0.006 \end{array}$	$\begin{array}{c} 0.322 \pm 0.002 \\ 0.295 \pm 0.030 \end{array}$	$\begin{array}{c} 0.561 \pm 0.015 \\ 0.539 \pm 0.012 \end{array}$

## Substitutivity



Do models support substitution of synonyms?

- Equal distributions in training data
- Only in 'primitive' condition in training data

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### Results Substitutivity

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Experiment	LSTMS2S	ConvS2S	Transformer
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Substitutivity, eq. distributed <sup>†</sup> primitive <sup>†</sup>		$\begin{array}{c} 0.962 \pm 0.005 \\ 0.612 \pm 0.027 \end{array}$	

# Substitutivity

Cosine distances

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	LSTMS2S	ConvS2S	Transformer
Equally distributed Primitive	0.389 0.408	0.142 0.461	0.079 0.373
Other	0.960	0.862	0.772

# Localism

Do models build representations incrementally?

append reverse A B C , copy D E  $\equiv$  append C B A , D E

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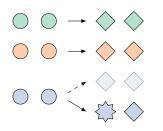
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Substitutivity, equally distributed <sup>†</sup> primitive <sup>†</sup>	$\begin{array}{c} 0.763 \pm 0.010 \\ 0.606 \pm 0.038 \end{array}$	$\begin{array}{c} 0.962 \pm 0.005 \\ 0.612 \pm 0.027 \end{array}$	$\begin{array}{c} 0.984 \pm 0.003 \\ 0.877 \pm 0.043 \end{array}$
Localism <sup>†</sup>	$0.447\pm0.007$	$0.574\pm0.044$	$0.561\pm0.025$

### Overgeneralisation



### Do models overgeneralise during training?

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### Results Overgeneralisation

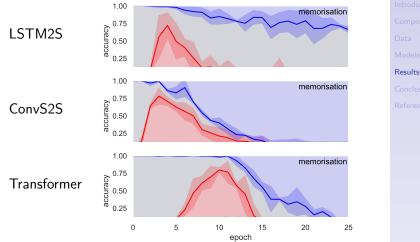
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PCFG SET*	$\textbf{0.769} \pm \textbf{0.006}$	$0.841\pm0.014$	$0.925\pm0.007$
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Localism <sup>†</sup>	$0.447\pm0.007$	$0.574\pm0.044$	$0.561\pm0.025$
Overgeneralisation*	$0.727\pm0.175$	$\textbf{0.783} \pm \textbf{0.116}$	$0.843\pm0.023$

# Overgeneralisation



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### Does a model find the right parts and rules?

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- Does a model find the right parts and rules?
- Does a model use the parts and rules it finds systematically



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- Does a model find the right parts and rules?
- Does a model use the parts and rules it finds systematically
- Does a model use the parts and rules it finds productively

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- Does a model find the right parts and rules?
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# The rest of the team



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Verna Dankers

Elia Bruni

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