

The compositionality of neural networks: integrating symbolism and connectionism

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The appropriateness of neural models

Testing
compositionality

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Compositionality

Data

Models

Results

Conclusion

References

- ▶ “Modern approaches [...] do not explicitly formulate and execute compositional paths” (Johnson et al., 2017)

The appropriateness of neural models

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

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- ▶ “Neural network models lack the ability to extract systematic rules” (Lake and Baroni, 2018)

The appropriateness of neural models

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- ▶ “They do not learn in a compositional way” (Liška et al., 2018)

The appropriateness of neural models

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- ▶ “[...] neural networks are essentially very large correlation engines that hone in on any statistical, potentially spurious pattern” (Hudson and Manning, 2018)

The appropriateness of neural models

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- ▶ “Neural network models lack the ability to extract systematic rules” (Lake and Baroni, 2018)
- ▶ “They do not learn in a compositional way” (Liška et al., 2018)
- ▶ “[...] neural networks are essentially very large correlation engines that hone in on any statistical, potentially spurious pattern” (Hudson and Manning, 2018)
- ▶ Neural networks are data-hungry because they don't develop re-usable representations (almost everyone)

The rest of the team

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References



Mathijs Mul



Verna Dankers



Elia Bruni

What is compositionality

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

The principle of compositionality

The meaning of a complex expression is determined by the meanings of its constituents and by its structure

Szabó (2000)

What is compositionality

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

The principle of compositionality

The meaning of a complex expression is determined by the meanings of its constituents and by its structure

Szabó (2000)

The meaning of a whole is a function of the meanings of the parts and of the way they are syntactically combined.

Partee (1995)

What is compositionality

What does it mean that neural networks are not compositional?

- ▶ They find different parts than we expect
- ▶ They find different rules than we expect
- ▶ They find other aspects of the data more salient
- ▶ They cannot represent hierarchy

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

What is compositionality

What does it mean that neural networks are not compositional?

- ▶ They find different parts than we expect
- ▶ They find different rules than we expect
- ▶ They find other aspects of the data more salient

- ▶ They favour modelling exceptions over learning rules
- ▶ They are not getting the right signal from the data
- ▶ The 'test' data is distributionally too different from the training data
- ▶ ...

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Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

Our approach: “dissect” compositionality:

- ▶ Does a model find the right parts and rules?

The appropriateness of neural models

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

Our approach: “dissect” compositionality:

- ▶ Does a model find the right parts and rules?
- ▶ Does a model use the parts and rules it finds *systematically*

The appropriateness of neural models

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

Our approach: “dissect” compositionality:

- ▶ Does a model find the right parts and rules?
- ▶ Does a model use the parts and rules it finds *systematically*
- ▶ Does a model use the parts and rules it finds *productively*

The appropriateness of neural models

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

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- ▶ Does a model find the right parts and rules?
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The appropriateness of neural models

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

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- ▶ Does a model prefer *rules* or *exceptions*?

Unary functions: reverse, swap, copy, ...

Binary functions: prepend, append, remove_first, ...

Characters: A, B, C, ...

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reverse A B C

Unary functions: reverse, swap, copy, ...

Binary functions: prepend, append, remove_first, ...

Characters: A, B, C, ...

reverse A B C \Rightarrow C B A

Unary functions: reverse, swap, copy, ...

Binary functions: prepend, append, remove_first, ...

Characters: A, B, C, ...

reverse A B C \Rightarrow C B A
copy D E

Unary functions: reverse, swap, copy, ...

Binary functions: prepend, append, remove_first, ...

Characters: A, B, C, ...

reverse A B C \Rightarrow C B A

copy D E \Rightarrow D E

Unary functions: reverse, swap, copy, ...

Binary functions: prepend, append, remove_first, ...

Characters: A, B, C, ...

reverse A B C \Rightarrow C B A

copy D E \Rightarrow D E

append C B A , D E

Unary functions: reverse, swap, copy, ...

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Characters: A, B, C, ...

reverse A B C	⇒	C B A
copy D E	⇒	D E
append C B A , D E	⇒	C B A D E

Unary functions: reverse, swap, copy, ...

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Characters: A, B, C, ...

reverse A B C \Rightarrow C B A

copy D E \Rightarrow D E

append C B A , D E \Rightarrow C B A D E

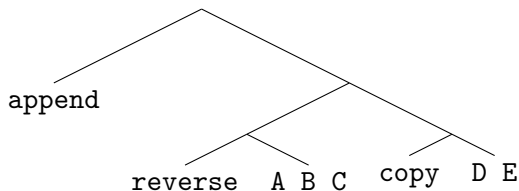
append reverse A B C , copy D E \Rightarrow C B A D E

Unary functions: reverse, swap, copy, ...

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append reverse A B C , copy D E \Rightarrow C B A D E



PCFG SET

Data Naturalisation

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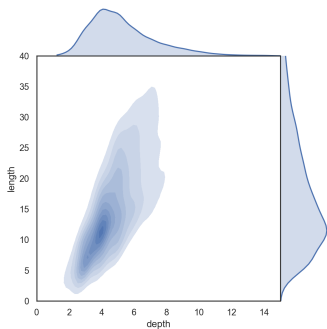
Data

Models

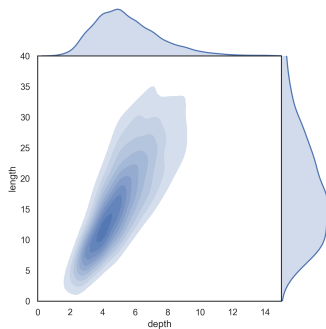
Results

Conclusion

References



(a) PCFG SET



(b) WMT 2017

Figure: Distribution of sentence depth and length in the PCFG SET and WMT2017 data.

1. **LSTMS2S** Recurrent encoder-decoder model with attention
2. **ConvS2S** Convolutional encoder and decoder with multistep attention
3. **Transformer** Fully attention based model

Results

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01

Systematicity

Testing
compositionality

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Compositionality

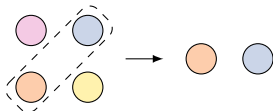
Data

Models

Results

Conclusion

References



Can models systematically recombine unseen pairs of functions?

Results

Systematicity

Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01
Systematicity*	0.51 ± 0.03	0.55 ± 0.01	0.70 ± 0.01

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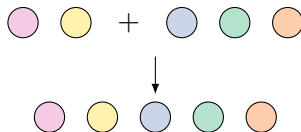
Data

Models

Results

Conclusion

References



Can models productively combine functions to generate longer sequences?

- ▶ Newly formed sequences (generalisation)
- ▶ Combinations of known sequences (concatenation)

Results

Productivity

Testing
compositionality

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Compositionality

Data

Models

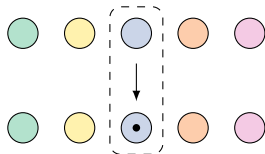
Results

Conclusion

References

Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01
Systematicity*	0.51 ± 0.03	0.55 ± 0.01	0.70 ± 0.01
Productivity, <i>generalisation</i> *	0.29 ± 0.01	0.32 ± 0.00	0.56 ± 0.02
<i>concatenation</i> †	0.20 ± 0.01	0.30 ± 0.03	0.54 ± 0.01

Substitutivity



Do models support substitution of synonyms?

- ▶ Equal distributions in training data
- ▶ Only in 'primitive' condition in training data

Results

Substitutivity

Testing
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Compositionality

Data

Models

Results

Conclusion

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Experiment	LSTMS2S	ConvS2S	Transformer
PCFG SET*	0.77 ± 0.01	0.84 ± 0.01	0.93 ± 0.01
Systematicity*	0.51 ± 0.03	0.55 ± 0.01	0.70 ± 0.01
Productivity, <i>generalisation</i> *	0.293 ± 0.01	0.32 ± 0.00	0.56 ± 0.02
<i>concatenation</i> [†]	0.20 ± 0.01	0.30 ± 0.03	0.54 ± 0.01
Substitutivity, <i>eq. distributed</i> [†]	0.76 ± 0.01	0.96 ± 0.01	0.98 ± 0.00
<i>primitive</i> [†]	0.61 ± 0.04	0.61 ± 0.03	0.88 ± 0.04

Substitutivity

Cosine distances

Testing
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Compositionality

Data

Models

Results

Conclusion

References

	LSTMS2S	ConvS2S	Transformer
<i>Equally distributed</i>	0.389	0.142	0.079
<i>Primitive</i>	0.408	0.461	0.373
<i>Other</i>	0.960	0.862	0.772

Localism

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Compositionality

Data

Models

Results

Conclusion

References

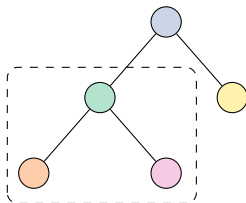


Figure: Localism

Do models build representations incrementally?

append reverse A B C , copy D E

\equiv

append C B A , D E

?

Results

Localism

Testing
compositionality

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Compositionality

Data

Models

Results

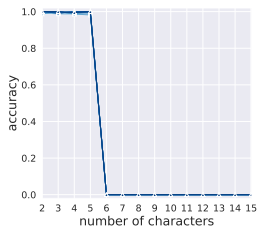
Conclusion

References

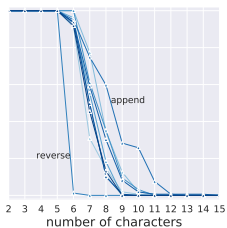
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Localism [†]	0.45 ± 0.01	0.57 ± 0.04	0.56 ± 0.03

Results

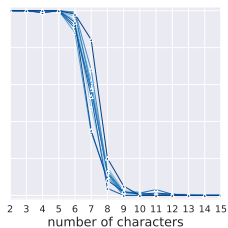
Generality of representations



(a) LSTM2S

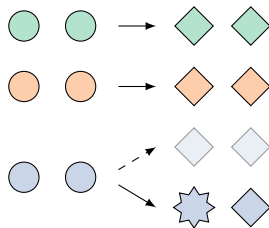


(b) Conv2S



(c) Transformer

Overgeneralisation



Do models overgeneralise during training?

Results

Overgeneralisation

Testing
compositionality

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Compositionality

Data

Models

Results

Conclusion

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Localism [†]	0.45 ± 0.01	0.57 ± 0.04	0.56 ± 0.03
Overgeneralisation*	0.73 ± 0.18	0.78 ± 0.12	0.84 ± 0.02

Overgeneralisation profile

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

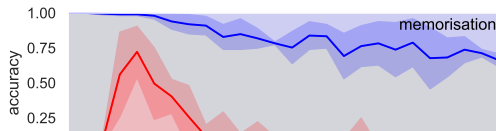
Models

Results

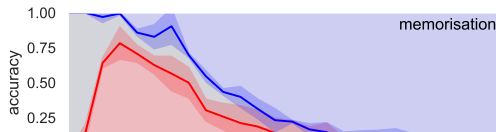
Conclusion

References

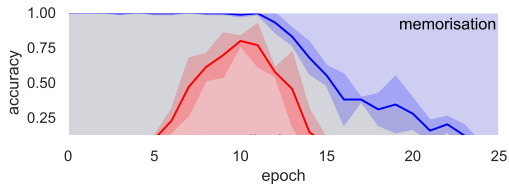
LSTM2S



ConvS2S



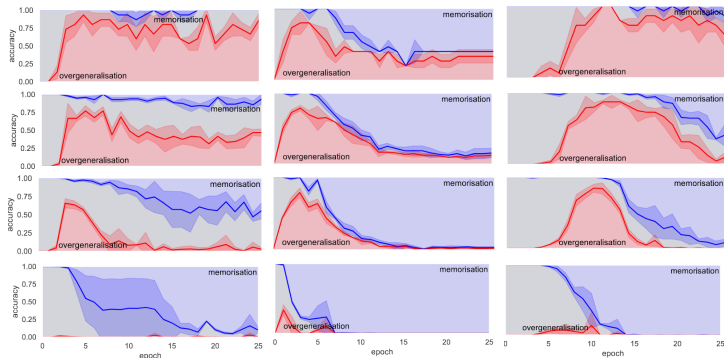
Transformer



Overgeneralisation

Different exception rates

Overgeneralisation profiles for exceptions occurring 0.01%, 0.05%, 0.1% and 0.5%



(a) LSTM2S

(b) Conv2S

(c) Transformer

Testing
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Compositionality

Data

Models

Results

Conclusion

References

Conclusion

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

- ▶ Does a model find the right parts and rules?

Conclusion

Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References

- ▶ Does a model find the right parts and rules?
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Conclusion

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Testing
compositionality

Dieuwke Hupkes

Compositionality

Data

Models

Results

Conclusion

References



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References

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